

Nonlinear Dose-Response Mechanisms Simulation with Bio-Mathematical Models

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Contents

- Introduction to the State Vector Model
- Detrimental bystander effects for chromosome aberrations
- Protective apoptosis-mediated BE for neoplastic transformation
- Update on studies with Two-Stage Cancer model



State Vector Model

For neoplastic transformation

initiation

via chromosome translocation

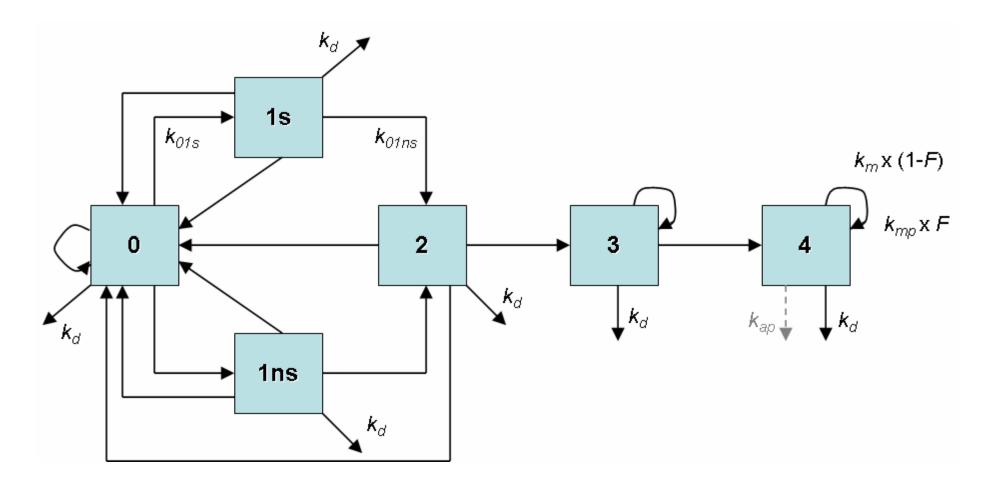
promotion

clonal expansion of I-cells loss of contact inhibition

- DSB repair
- cell killing dose rate dependent



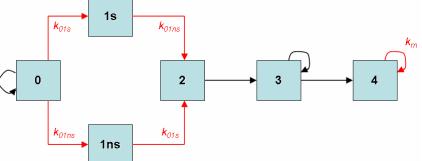
State Vector Model





Detrimental bystander effects

- Included in a dose-dependent way strongest effect at low doses
- New bystander rates:



- 1) $k_{01b_by} \times \exp(-\lambda_{1by} \times D)$
- 2) $k_{01r_{by}} \times DR \times \exp(-\lambda_{2by} \times D)$
- 3) $(1+k_{m_{by}} \times \exp(-\lambda_{2by} \times D))$
- $k_{01b_by} = k_{01r_by} = k_{m_by} = 0$ at D = 0

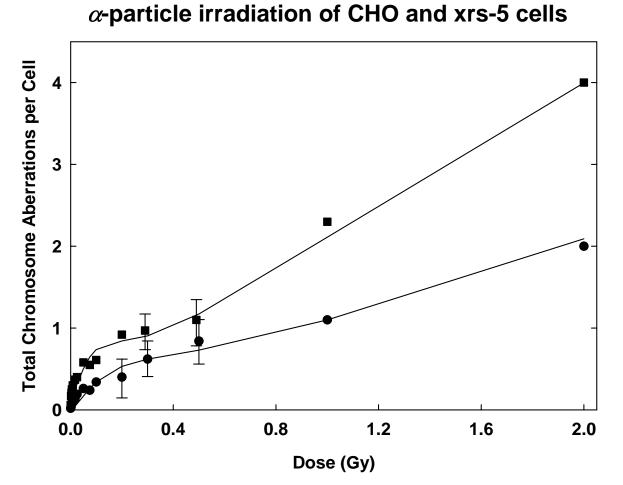


Data by Nagasawa and Little Mutation Research 2002

- CHO and xrs-5 cells, α-particles, total chromosome aberrations
- First, fit model without BE to control and high dose data
- Then, fit model with BE to all data



Data by Nagasawa and Little





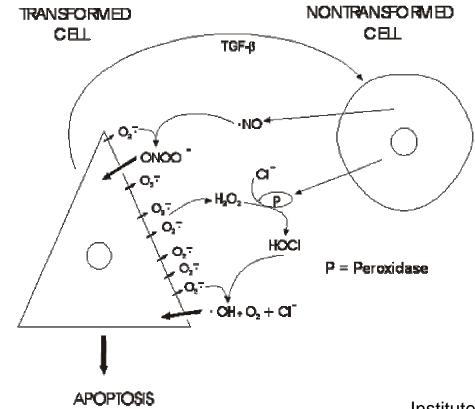
Fit results

- Approaches 1) and 3) worked equally well
- Approach 2) did not work → initiation due to BE is mostly post-exposure (as expected)
- To fit xrs-5 data apply reduction factor for DSB repair rates



Bystander-induced apoptosis

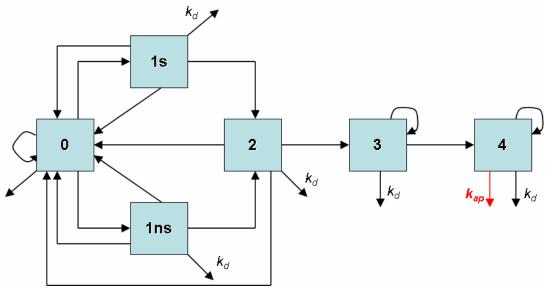
- Is a protective effect
- Dr. Georg Bauer (Anticancer Res 2000)





Bystander-induced apoptosis For low-LET radiation

- Protective Apoptosis-Mediated process (PAM),
 B.R. Scott et al. (2003)
- PAM can eliminate cells in State 4





Bystander-induced apoptosis

- PAM = 0 at D = 0
- PAM = 0 during irradiation
- PAM activated by 1 mGy low-LET radiation
- PAM activated for various times after irradiation
- PAM effective at low doses –
 no effect at *D* > 200 mGy



Data by Redpath et al. Radiat. Res. 2001

- CGL1 cells, γ-rays, neoplastic transformation
- Irradiation period: 3.3 mGy/min for $D \le 100$ mGy cell doubling time of 20 hrs
- 1 day holding period: 20 hrs
- 10 days exponential growth: 20 hrs
- Confluent growth until day 26: 38 days





Fit approach

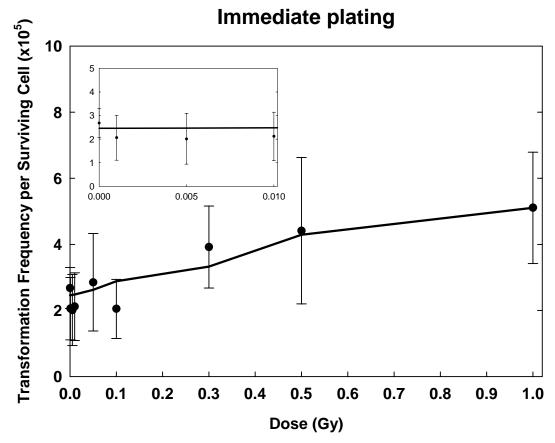
• TF/SC =
$$\frac{N_4(t_{end})}{N_0(t_{end}) + N_{1s}(t_{end}) + N_{1ns}(t_{end}) + N_2(t_{end}) + N_3(t_{end}) + N_4(t_{end})}$$

- Fit model without PAM to control and high dose data for immediate and delayed plating simultaneously
- Forward simulation without PAM to all data points for immediate plating
- Fit model with PAM to all data points for delayed plating
 1 free parameter: k_{ap}

2 free parameters: k_{ap} and $t_{ap off}$

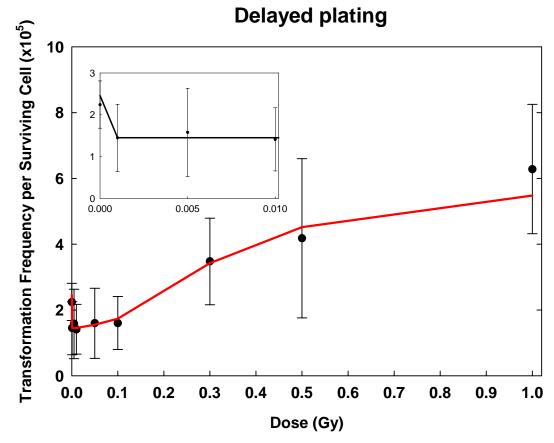


Data by Redpath et al. Forward simulation





Data by Redpath et al. Fit with two free parameters





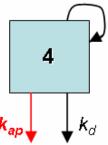
Fit results

 k_{ap} = 0.024/day → How many State 4 cells killed at day 26 after 100 mGy?

Simulation performed starting with 1 cell:

 $N_4(26) - N_4(26; k_{ap}=0) = 9$ cells

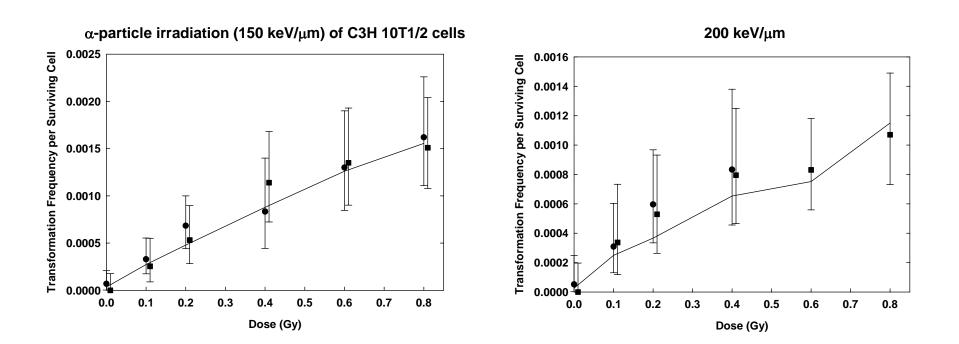
 $N_0(26) + N_{1s}(26) + \ldots + N_4(26) = 8.10^5$



 t_{ap_off} = 22 days Jamali and Trott (1996): two week induction of apoptosis after 1 Gy X-irradiation



Data by Miller et al. Radiat. Res. 1995



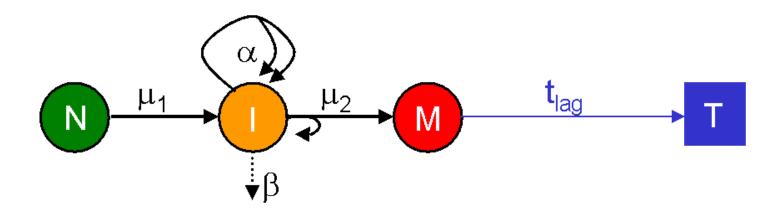


Conclusions

- SVM can describe detrimental and protective bystander effects
- The experimentally proven phenomenon of bystander-induced apoptosis can explain protective effects of low doses of low-LET radiation
- SVM can also explain LNT-shaped data sets
- Work towards a model than contains all essential mechanisms that work at low doses: inducible repair and radical scavenging, bystander effects ...



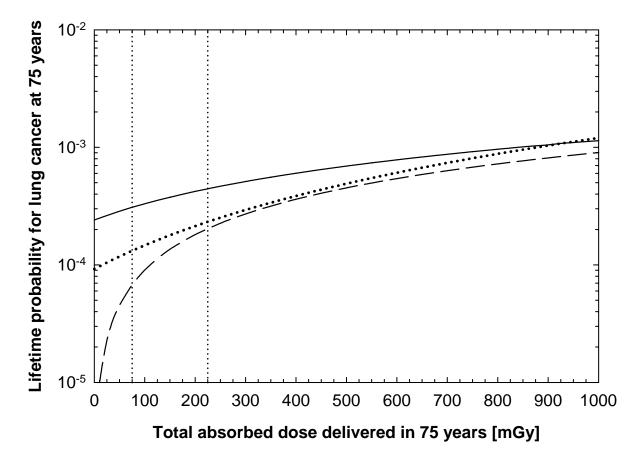
TSCE model with clonal expansion



- Four age-independent stochastic rates (μ_1 , μ_2 , α , β)
- μ₁ a function of dose-rate also included endogenous DNA damage

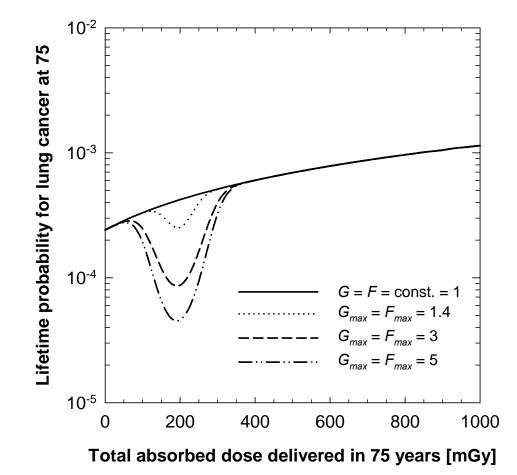


Lifetime probability for lung cancer Low-LET radiation at low dose rates



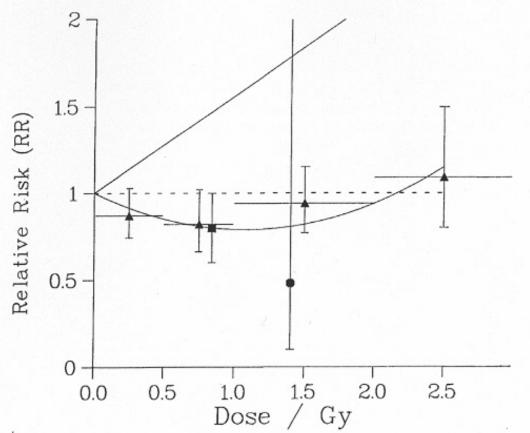


Lifetime probability for lung cancer With repair and scavenger induction





Rossi and Zaider: "Radiogenic lung cancer: the effects of low doses of low LET radiation" REB 1997

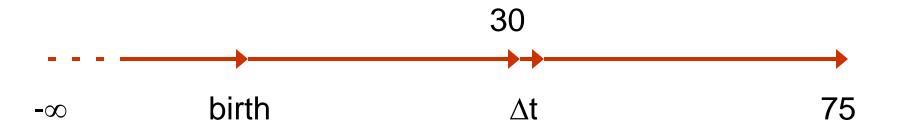




Mutation models for high dose rates

Rate of change in the expected number of simple or complex lesions per cell at time *t*

$$\frac{dL_{i}(t)}{dt} = \Sigma_{i}^{endo} + \Sigma_{i}^{rad} D - \lambda_{i}L_{i}(t)$$



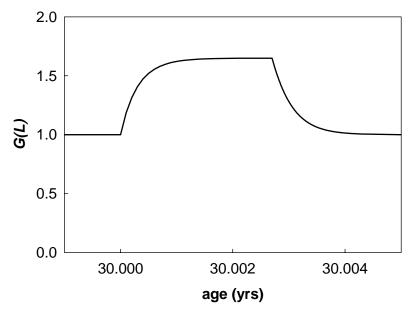


$$\mu_1(t) \propto \frac{\varphi_{sl}}{G(L_{sl})} \lambda_{sl} L_{sl}(t) + \frac{\varphi_{cl}}{G(L_{cl})} \lambda_{cl} L_{cl}(t)$$

 φ_i probability *i*th type (simple or complex) of lesion is misrepaired

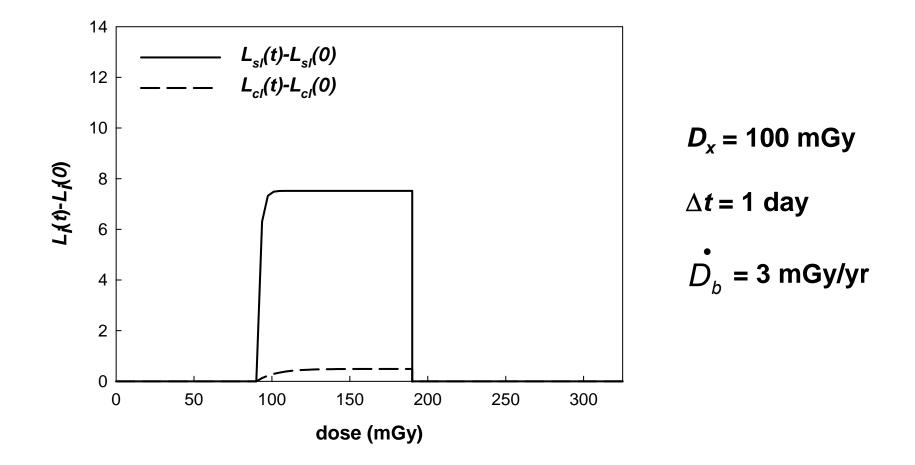
Misrepair probability modified with..

$$G(L) = 1 + \delta \left[1 - e^{-\gamma \Delta L(t)} \right]$$



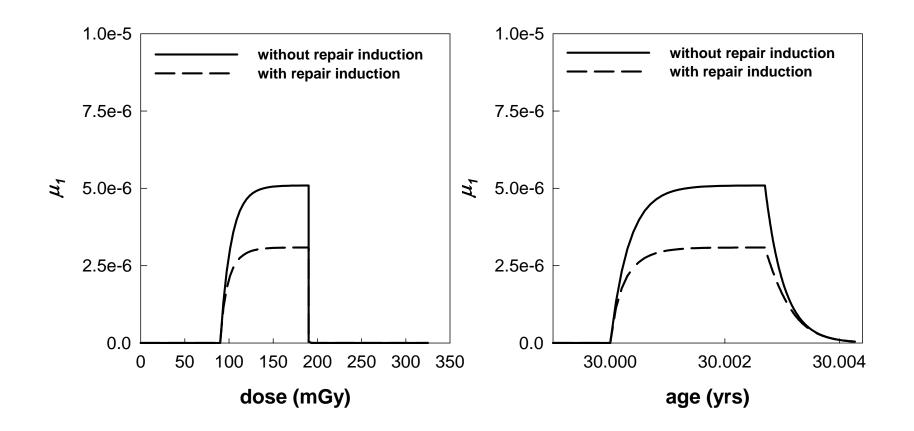


$$G(L) = 1 + \delta \left[1 - e^{-\gamma \Delta L(t)} \right]$$





$$\mu_1(t) \propto \frac{\varphi_{sl}}{G(L_{sl})} \lambda_{sl} L_{sl}(t) + \frac{\varphi_{cl}}{G(L_{cl})} \lambda_{cl} L_{cl}(t)$$





Acknowledgements

- Collaborator: Dr. Robert D. Stewart
- Austrian Science Foundation FWF (project P18055-N02)
- RISC-RAD project, EC Contract No. FI6R-CT-2003-508842
- EU Marie Curie Individual Fellowship, EC Contract No. FIGH-CT-2002-50513
- Marie Curie European Reintegration Grant, EC Contract No. MERG-CT-2004-006610
- Atomic Energy of Canada Limited
- US Department of Energy, Grant Nos. DE-FG02-03ER63541 and DE-FG02-03ER63665



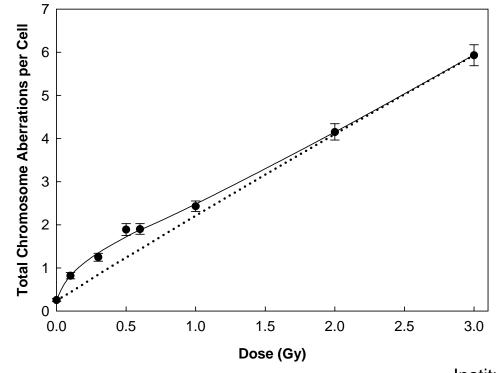






Data by Durante et al. IJRB 1992

- Supralinearity assumed to be HRS
- SVM repair rates divided by $1 + \lambda_{red} \times exp(-\lambda_{decr} \times D)$





Data by Redpath et al.

Fit of control and high dose data for immediate and delayed plating simultaneously

